

DOCUMENT RESUME

ED 325 527

TM 015 788

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TITLE Measuring Second-Order Factors Using Confirmatory Methods: A Case Study Example with the Hendrick-Hendrick Love Instrument.
PUB DATE Nov 90
NOTE 26p.; Paper presented at the Annual Meeting of the Mid-South Educational Research Association (19th, New Orleans, LA, November 15, 1990).
PUB TYPE Speeches/Conference Papers (150)
EDRS PRICE MF01/PC02 Plus Postage.
DESCRIPTORS Case Studies; Data Analysis; *Factor Analysis; *Graduate Students; Heuristics; Higher Education; Mathematical Models; *Measurement Techniques; *Undergraduate Students; Validity
IDENTIFIERS *Confirmatory Factor Analysis; Hendrick Hendrick Love Instrument; *Second Order Factors

ABSTRACT

The application and utility of confirmatory second-order factor analytic methods are discussed. Factor analysis is central to concerns regarding measurement validity. Confirmatory methods are especially useful because they explicitly consider measurement error influences and because the methods are inherently theory-driven and theory-oriented. Second-order confirmatory methods, which have not been applied with great frequency in the literature, allow the researcher to explore more thoroughly a reality that may be just as complex as are other formulated models. To make the explanation of applying confirmatory second-order methods more concrete, a data set involving responses of 487 undergraduates and graduate students (representing three pooled samples from previous research studies) to the Hendrick-Hendrick love instrument was analyzed for heuristic purposes. Two tables contain data from the study. Two appendices contain seven additional tables related to the analysis. A 31-item list of references is included. (Author/SLD)

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MEASURING SECOND-ORDER FACTORS USING CONFIRMATORY METHODS:
A CASE STUDY EXAMPLE WITH THE HENDRICK-HENDRICK LOVE INSTRUMENT

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ABSTRACT

The present study illustrates the application, and the utility, of confirmatory second-order factor analytic methods. Factor analysis is central to concerns regarding measurement validity. Confirmatory methods are especially useful, because they explicitly consider measurement error influences, and because the methods are inherently theory-driven and theory-oriented. Second-order confirmatory methods, not applied with great frequency in the literature, offer the promise of allowing the researcher to explore more thoroughly a reality which many see as being just as complex as some of the models that we have been led to formulate. To make the explanation of applying confirmatory second-order methods more concrete, a data set involving responses of 487 subjects to the Hendrick-Hendrick love instrument is analyzed for heuristic purposes.

Factor analytic studies of measurement integrity are important, as Nunnally (1978, pp. 111-112) notes:

construct validity has been spoken of as "trait validity" and "factorial validity".... Factor analysis is intimately involved with questions of validity... Factor analysis is at the heart of the measurement of psychological constructs.

Gorsuch (1983, pp. 350-351, emphasis added) concurs, noting that "A prime use of factor analysis has been in the development of both the theoretical constructs for an area and the operational representatives for the theoretical constructs." Similarly, C. Hendrick and S. Hendrick (1986, p. 393) note that "theory building and construct measurement are joint bootstrap operations." Factor analysis at once both tests measurement integrity and sheds light on underlying theory. Confirmatory factor analytic methods are particularly important, because these methods overcome the tendency of exploratory methods to capitalize on error. However, confirmatory factor analytic methods do tend to require fairly large sample sizes (Baldwin, 1989).

Second-order factor analytic methods can yield especially useful insights for some problems, but are little understood and are somewhat infrequently applied by researchers (Thompson, Webber & Berenson, 1990). Many researchers are familiar with the extraction of principal components principal factors from either a variance-covariance matrix or a correlation matrix. However, the factors extracted from such matrices, called first-order factors,

can be rotated obliquely such that the rotated factors themselves are correlated. This interfactor matrix can then, in turn, also be subject to factor analysis. These "higher order" factors would be termed second-order factors. As Kerlinger (1984, p. xiv) noted, "while ordinary factor analysis is probably well understood, second-order factor analysis, a vitally important part of the analysis, seems not to be widely known and understood." Example applications of second-order factor analysis are reported by Kerlinger (1984), Thompson and Borrello (1986), and by Thompson and Miller (1981). Thompson (1990) offers a program that automates exploratory second-order analysis.

Logically, if confirmatory factor analytic methods are useful, and if second-order methods are useful, the combination of these methods might also prove useful. The combination was very briefly alluded to by Joreskog and Sorbom (1986, p. I.11). Marsh and his colleagues (Marsh, 1985; Marsh & Hocevar, 1985, 1988; Marsh & Richards, 1987) has elaborated this application. The purpose of the present paper was to illustrate the potential utility of combining confirmatory and second-order methods, and to illustrate the mechanics of the analysis. To make the discussion concrete, the application is illustrated using real data not previously analyzed using confirmatory second-order methods.

Heuristic Example

Behavioral scientists have traditionally eschewed scholarly inquiry regarding love phenomena. As Wrightsman and Deaux (1981, p. 170) observe, researchers have historically "believed that love

is too mysterious and too intangible for scientific study." Initial investigations of love phenomena conducted during the 1940s were "followed by nearly a 20-year period in which there is almost no published evidence of efforts to investigate love phenomena using inventories or paper-and-pencil testing" (Elkins & Smith, 1979, p. 10). For example, Curtin (1973) found that love was not mentioned in the 23 volumes of the Annual Review of Psychology that he surveyed. However, as C. Hendrick and S. Hendrick (1986, p. 392) note, "During the past decade, love has become respectable as an area for study by psychologists." Work by Rubin (1984), by Sternberg and Grajek (1984), and by Tennov (1979) illustrates efforts to develop science in the area of love phenomena.

One series of studies of love has been inductive (Thompson & Borrello, 1990). Another series of studies has been deductively grounded (Borrello & Thompson, 1990, in press; C. Hendrick & S. Hendrick, 1986, in press; S. Hendrick & C. Hendrick, 1987; C. Hendrick, S. Hendrick, Foote & Slapion-Foote, 1984) in Lee's (1973/1976) typology of three primary love styles: (a) *eros*, which is romantic or passionate love, (b) *ludus*, which is game playing love, and (c) *storge*, which is friendship love. Lee suggests that three secondary styles are formed as compounds of the primary styles, but still have their own unique properties and characters: (d) *mania*, which is a compound of *ludus* and *eros*, (e) *pragma*, which is a compound of *storge* and *ludus*, and (f) *agape*, which is a compound of *eros* and *storge*.

In at least three major studies with discrete and large

cohorts of subjects Hendrick and Hendrick have consistently found that their measure yields a six-dimensional orthogonal structure corresponding to the elements of Lee's (1973/1976) typology. However, Lee's model might be interpreted as being hierarchical, and one appropriate test of the model would employ hierarchical factor analysis, as against the conventional nonhierarchical factor analytic methods used in most of the previous studies, and to implement the analysis using confirmatory methods.

Method

Subjects

Subjects in the study were 487 undergraduate and graduate students who have participated in previous studies (Borrello & Thompson, 1987, 1989a, 1989b; Thompson & Borrello, 1987) focusing on a measure other than C. Hendrick and S. Hendrick's (1986, in press). However, as part of one study (Thompson & Borrello, 1987) 260 subjects completed the 18 items, three per factor for each of the six factors, that were most highly correlated with the structure isolated by C. Hendrick and S. Hendrick (1986). In other studies 227 (176 + 51) subjects completed the same 18 items from the Hendrick-Hendrick measure and two additional items from the measure. These two items measure the Agape and Mania constructs in the Lee typology. For the purposes of the present study these three samples were pooled. Table 1 presents the demographic characteristics of the samples.

INSERT TABLE 1 ABOUT HERE.

Analysis

The analysis in the present study was implemented using LISREL (Joreskog & Sorbom, 1986) to fit a second-order model to the data ($n=487$) based on the interitem correlation matrix. The variance-covariance matrix is certainly another sensible candidate for analysis, and the same basic logic is applied in such an analysis. Four matrices are estimated in a second-order analysis.

The first matrix is the first-order factor matrix, called "LAMBDA X" in LISREL. This matrix has y rows, corresponding to the number of variables. In the present example, y was 18. The number of columns in the matrix equals the number of first-order factors posited plus the number of second-order factors posited. The illustrative model posited the existence of the six dimensions named by Lee (1973/1976). Each first-order factor was "marked" by three variables. One second-order (potentially "G") factor was presumed in the model tested, i.e., it was posited that all six first-order factors might be associated with a single higher-order factor, as suggested by findings in some previous research (e.g., Sternberg & Grajek, 1984) isolating "G" or general factor dynamics.

Usually it is wise to isolate factor positions with several variables, so that factor positions are more fully constrained. So that the model will be mathematically "identified", one coefficient per first-order factor is fixed with a value of 1.0. Typically, in every y by $f+g$ "LAMBDA Y" matrix, f entries are constrained to be ones, $y-f$ entries are free to be estimated based on the data in hand, and $(y \text{ times } f+g)-y$ entries are constrained to be zeroes.

Thus, in the present example, $f=6$ entries were fixed to be ones, 12 ($y=18$ minus $f=6$) entries were free to be estimated, and 108 ($y=18$ times $f=6+g=1$ minus $y=18$) entries were fixed to be zeroes.

The second matrix is the second-order factor matrix, called "BETA" in LISREL. This matrix has $f+g$ rows and columns. Typically, g entries are constrained to be ones so that the model is mathematically "identified", $f-g$ entries are free to be estimated based on the data in hand, and $(f+g \text{ times } f+g)-f$ entries are constrained to be zeroes. Thus, in the present example, $g=1$ entry was fixed to be a one, 5 ($f=6$ minus $g=1$) entries were free to be estimated, and 43 ($f+g=7$ times $f+g=7$ minus $f=6$) entries were fixed to be zeroes.

The third matrix is the factor variance matrix, called "PSI" in LISREL. This is a triangular matrix with $f+g$ diagonal entries and $(f+g \text{ times } f+g-1)/2$ unique off-diagonal entries. Typically, the off-diagonal entries will be fixed to be zeroes and the diagonal entries are estimated. Thus, in the present study $f+g=7$ entries in the "PSI" matrix were estimated.

The fourth matrix is a one-dimensional array of length y . This matrix estimates the combination of both the measurement error and the unique variances associated with each variable. These entries are akin to ones minus the communality coefficients in exploratory factor analysis. If this matrix is constrained to consist of zeroes, a model analogous to a principal components model is being evaluated. Typically, the entries in this matrix are set free to vary, as they were here.

Table 2 presents the model fit to the data for the 487 subjects. With 129 degrees of freedom, the chi-square goodness of fit statistic was 390.14. The fit index was .912, while the adjusted fit index was .884. These results suggest that the model is plausible, though reasonable fit never rules out that possibility that alternative models may also fit the data.

INSERT TABLE 2 ABOUT HERE.

Discussion

The Table 2 data can be consulted to illustrate both the mechanics of the interpretation process, and the potential utility of confirmatory second-order methods. There have been some indications in previous research with other measures (cf. Sternberg & Grajek, 1984; Borrello & Thompson, 1989a) that a "G" or general factor dominates the factor space underlying love, and that other factors exist as thematic variation about this overriding dimension. Given that the model was a reasonable fit to the data, the second-order analysis can be consulted to explore this issue.

The standard errors of the estimates can be consulted to facilitate interpretation of the maximum-likelihood estimates presented in Table 2. Most of the standard errors for the "LAMBDA Y" estimates were about .08; the largest standard error (.161) was for item 14, a Ludus item, which had a "LAMBDA" estimate of .940. Most of the standard errors of the "BETA" estimates were about .09; the largest standard error (.130) was for the Agape factor, which involved an estimate of .785. The standard errors associated with

the "PSI" matrix ranged from .053 (Agape) to .180 (Storge). Since the estimates were uniformly several times their standard errors, all the estimates presented in Table 2 warrant attention during interpretation.

The "BETA" coefficients for Mania and Agape (and to some extent for Pragma) for the second-order factor suggest that a fairly dominant Mania-Agape combination underlies the structure. The entries in the "PSI" matrix confirm this impression. As Marsh and Hocevar (1985, p. 570) explain, "When a lower order factor is incorporated into a higher order factor, the diagonal of psi is a factor residual; otherwise, the diagonal value of psi is a factor variance."

A residual first-order factor variance of .922 suggests that Storge does not play much of a role in the second-order factor. The relatively small residual factor variances for Mania (.104) and Agape (.246) suggest that the second-order factor contains a goodly portion of these two first-order factors. The variance of the second-order factor (.420) is also itself commensurate with the residual variances for first-order factors Ludus (.423), Pragma (.439), and Eros (.530).

Taken together, these results appear supportive of a model of love positing the existence of a Mania-Agape factor somewhat dominating the factor space in the presence of several more thematic factors. This view is consistent with some findings in studies employing different measures and different analytic methods (e.g., Sternberg & Grajek, 1984).

In summary, the present study has illustrated the application, and hopefully the utility, of confirmatory second-order factor analytic methods. Confirmatory methods are useful, because they explicitly consider measurement error influences, and because the methods are inherently theory-driven and theory-oriented. Second-order confirmatory methods offer the promise of allowing the researcher to explore more thoroughly a reality which many see as being just as complex as some of the models that we have been led to formulate.

References

- Baldwin, B. (1989). A primer in the use and interpretation of structural equation models. Measurement and Evaluation in Counseling and Development, 22, 100-112.
- Borrello, G.M., & Thompson, B. (1987, November). Construct validity of a measure of love relationships perceptions. Paper presented at the annual meeting of the Mid-South Educational Research Association, Mobile, AL.
- Borrello, G., & Thompson, B. (1989a). A replication "bootstrap" analysis of the structure underlying perceptions of stereotypic love. Journal of General Psychology, 116, 317-327.
- Borrello, G., & Thompson, B. (1989b, November). Second-order factor analysis as a validity assessment tool: A case study example involving perceptions of stereotypic love. Paper presented at the annual meeting of the Mid-South Educational Research Association, Little Rock, AR. (ERIC Document Reproduction Service No. ED 312 299)
- Borrello, G.M., & Thompson, B. (1990). An hierarchical analysis of the Hendrick-Hendrick measure of Lee's typology of love. Journal of Social Behavior and Personality, 3, 327-342.
- Borrello, G.M., & Thompson, B. (in press). A note regarding the validity of Lee's typology of love. Journal of Psychology.
- Curtin, M. E. (1973). Symposium on love. New York: Behavioral Publications.
- Elkins, G. R., & Smith, D. (1979). Meaning and measurement of love: A review of humanistic and behavioral approaches. The Humanist

Educator, 18(1), 7-14.

Gorsuch, R.L. (1983). Factor analysis (2nd ed). Hillsdale, NJ: Erlbaum.

Hendrick, C., & Hendrick, S. (1986). A theory and method of love. Journal of Personality and Social Psychology, 50, 392-402.

Hendrick, C., & Hendrick, S.S. (in press). A relationship-specific version of the Love Attitudes Scale. Journal of Social Behavior and Personality.

Hendrick, C., Hendrick, S., Foote, F. H., & Slapion-Foote, M. J. (1984). Do men and women love differently? Journal of Social and Personal Relationships, 1, 177-195.

Hendrick, S.S., & Hendrick, C. (1987). Love and sex attitudes: A close relationship. In W.H. Jones & D. Perlman (Eds.), Advances in personal relationships (Vol. 1) (pp. 141-169). Greenwich, CT: JAI Press.

Joreskog, K.G., & Sorbom, D. (1986). LISREL 6: Analysis of linear structural relationships by maximum likelihood, instrumental variables, and least squares methods (4th ed.). Mooresville, IN: Scientific Software.

Kerlinger, F.N. (1984). Liberalism and conservatism: The nature and structure of social attitudes. Hillsdale, NJ: Erlbaum.

Lee, J. A. (1973). The colors of love: An exploration of the ways of loving. Don Mills, Ontario: New Press. (Popular Edition, 1976)

Marsh, H.W. (1985). The structure of masculinity/femininity: An application of confirmatory factor analysis to higher-order

factor structures and factorial invariance. Multivariate Behavioral Research, 20, 427-449.

Marsh, H.W., & Hocevar, D. (1985). Application of confirmatory factor analysis to the study of self-concept: First- and higher order factor models and their invariance across groups. Psychological Bulletin, 97, 562-582.

Marsh, H.W., & Hocevar, D. (1988). A new, more powerful approach to multitrait-multimethod analyses: Application of second-order confirmatory factor analysis. Journal of Applied Psychology, 73, 107-117.

Marsh, H.W., & Richards, G.E. (1987). The multidimensionality of the Rotter I-E scale and its higher-order structure: An application of confirmatory factor analysis. Multivariate Behavioral Research, 22, 39-69.

Nunnally, J. (1978). Psychometric theory (2nd ed.) New York: McGraw-Hill.

Rubin, Z. (1984). Toward a science of relationships. Contemporary Psychology, 29, 856-858.

Sternberg, R. J., & Grajek, S. (1984). The nature of love. Journal of Personality and Social Psychology, 47, 312-329.

Tennov, D. (1979). Love and limerance: The experience of being in love. New York: Stein and Day.

Thompson, B. (1990). SECONDO: A program that computes a second-order principal components analysis and various interpretation aids. Educational and Psychological Measurement, 50, 575-580.

Thompson, B., & Borrello, G.M. (1986). Second-order factor

structure of the MBTI: A construct validity assessment. Measurement and Evaluation in Counseling and Development, 18, 148-153.

Thompson, B., & Borrello, G. (1987). Concurrent validity of a love relationships scale. Educational and Psychological Measurement, 47, 985-995.

Thompson, B., & Borrello, G.M. (1990, March). Different views of love: Deductive and inductive inquiry and the implications of research findings for counseling. Paper presented at the annual meeting of the American Association for Counseling and Development, Cincinnati. (ERIC Document Reproduction Service No. ED 315 713)

Thompson, B., & Miller, A.H. (1981). The utility of "Social Attitudes" theory. Journal of Experimental Education, 49, 157-160.

Thompson, B., Webber, L., & Berenson, G.S. (1990, January). Validity of a measure of children's health locus of control: A second-order factor analysis. Paper presented at the annual meeting of the Southwest Educational Research Association, Austin, TX.

Wrightsman, L. S., & Deaux, K. (1981). Social psychology in the 80s. Monterey, CA: Brooks/Cole.

Table 1
Sample Demographic Characteristics

Study	Mean Age	n Female	n
	^a		
Borrello & Thompson (1987)	32.9 (5.5)	135(76.7%)	176
Thompson & Borrello (1987)	35.4 (7.1)	207(79.6%)	260
New subjects added by Borrello & Thompson (1989a)	36.1(11.0)	34(66.7%)	51
Total	35.0 (7.5)	376(77.2%)	487

^aStandard deviations are presented in parentheses next to means.

Table 2
Confirmatory Second-Order Solution
($n=487$, $y=18$)

LAMBDA γ Item	LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE	LOVE G
Eros 2	.000	.838	.000	.000	.000	.000	.000
Ludus 8	1.000	.000	.000	.000	.000	.000	.000
Storge18	.000	.000	1.000	.000	.000	.000	.000
Pragma25	.000	.000	.000	.000	1.000	.000	.000
Mania 33	.000	.000	.000	.887	.000	.000	.000
Agape 38	.000	.000	.000	.000	.000	1.000	.000
Pragma27	.000	.000	.000	.000	.636	.000	.000
Eros 4	.000	1.000	.000	.000	.000	.000	.000
Storge21	.000	.000	.602	.000	.000	.000	.000
Agape 39	.000	.000	.000	.000	.000	.985	.000
Mania 32	.000	.000	.000	1.000	.000	.000	.000
Ludus 14	.940	.000	.000	.000	.000	.000	.000
Agape 42	.000	.000	.000	.000	.000	.979	.000
Mania 31	.000	.000	.000	.881	.000	.000	.000
Pragma26	.000	.000	.000	.000	.548	.000	.000
Storge20	.000	.000	.336	.000	.000	.000	.000
Ludus 9	.609	.000	.000	.000	.000	.000	.000
Eros 7	.000	.670	.000	.000	.000	.000	.000
BETA							
	LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE	LOVE G
LUDUS	.000	.000	.000	.000	.000	.000	.246
EROS	.000	.000	.000	.000	.000	.000	.327
STORGE	.000	.000	.000	.000	.000	.000	.175
MANIA	.000	.000	.000	.000	.000	.000	1.000
PRAGMA	.000	.000	.000	.000	.000	.000	.524
AGAPE	.000	.000	.000	.000	.000	.000	.785
LOVE G	.000	.000	.000	.000	.000	.000	.000
PSI							
	LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE	LOVE G
LUDUS	.423						
EROS	.000	.530					
STORGE	.000	.000	.922				
MANIA	.000	.000	.000	.104			
PRAGMA	.000	.000	.000	.000	.439		
AGAPE	.000	.000	.000	.000	.000	.246	
LOVE G	.000	.000	.000	.000	.000	.000	.420

Note. Entries of ".000" were all constrained or fixed to be zeroes; entries of "1.000" were all fixed to be ones; all other results were maximum-likelihood estimates that were considered "free" in the model fit to the data.

Appendix A:
R Matrices for 18 Items Administered to 487 Subjects (Below Diagonal)
and for 20 Items for a Subsample of 227 Subjects (Above Diagonal)

Item	2E	8L	18S	25P	33M	38A	27P	4E	21S	39A	32M	14L	42A	31M	26P	20S	9L	7E	37A	34M
2E	-127	117	007-063	062-055	486	131	131	042-133	111-024	132	006-047	348	155	087						
8L	-140		061	141	244-049	205-212	054-146	133	414-172	169	060	026	340	030-129	012					
18S	056	079		043	012-068	110	065	584	117	073-094-044-015	184	248	038	027	040-056					
25P	-002	156	122		205	098	302-016-001	101	135	148	066	151	234	109	061	141	017-041			
33M	028	236	033	210		261	121-015-051	253	470	140	219	410	128-039	221	052	240	128			
38A	069-044	000	194	306		072	099	007	471	288	020	499	124	018-025	009	071	427	068		
27P	-094	206	090	365	130	089	-049	098	064	194	208-013	114	122	064	137	012-061	036			
4E	491-152	022	049	061	128-076			056	228	060-199	193	024	222	054-033	423	250	144			
21S	120	032	563	066	040	067	015	097		177-054-056-005-044	159	118-045-056	026-063							
39A	225-088	126	130	263	502	085	254	200		391	012	527	119	138-045	046	146	457	119		
32M	087	153	081	172	446	348	196	061	020	381		056	340	448	117-027	126	103	247	225	
14L	-116	420-011	098	147	004	199-176-048	015	121		004	136-094-038	258	020-092	022						
42A	180-146	029	160	230	496-004	254	110	481	365	030		247	039-050-073	122	548-025					
31M	046	165	005	163	443	244	112	080	028	217	457	173	331		045-100	121	017	140	004	
26P	132	081	160	305	095	124	150	240	177	193	109-040	151	141		269	126	177	155	085	
20S	-001-022	315	118-080	024	083	009	184-016-028-082	004-144	103		069	133	025-036							
9L	-069	277	064	040	174-026	179-074-016	000	041	257-094	040	065	084		064-066	185					
7E	310	067	018	132	176	165	055	378	022	164	159	018	102	112	143	056	022		179	135
37A																				072

Note. The item names indicate the number of each item in the Hendrick-Hendrick measure, and subscale membership is reported as the alphabetic code following each item number. The abbreviations are: "A" = Agape; "E" = Eros; "L" = Ludus; "M" = Mania; "P" = Pragma; and "S" = Storge. Thus, item "2E" was the second item from the Hendrick-Hendrick measure and was associated with the Eros subscale in their studies.

Appendix B.1
Confirmatory First-Order Solution Positing Uncorrelated Factors
(n=487, y=18)

LAMBDA X Item	LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE
Eros 2	.000	.635	.000	.000	.000	.000
Ludus 8	.673	.000	.000	.000	.000	.000
Storge18	.000	.000	.992	.000	.000	.000
Pragma25	.000	.000	.000	.000	.859	.000
Mania 33	.000	.000	.000	.658	.000	.000
Agape 38	.000	.000	.000	.000	.000	.720
Pragma27	.000	.000	.000	.000	.424	.000
Eros 4	.000	.774	.000	.000	.000	.000
Storge21	.000	.000	.573	.000	.000	.000
Agape 39	.000	.000	.000	.000	.000	.697
Mania 32	.000	.000	.000	.678	.000	.000
Ludus 14	.625	.000	.000	.000	.000	.000
Agape 42	.000	.000	.000	.000	.000	.609
Mania 31	.000	.000	.000	.674	.000	.000
Pragma26	.000	.000	.000	.000	.354	.000
Storge20	.000	.000	.321	.000	.000	.000
Ludus 9	.411	.000	.000	.000	.000	.000
Eros 7	.000	.488	.000	.000	.000	.000

MEASURES OF GOODNESS OF FIT FOR THE WHOLE MODEL:
 CHI-SQUARE WITH 135 DEGREES OF FREEDOM IS 585.40 (PROB.
 LEVEL = .000)
 GOODNESS OF FIT INDEX IS .881
 ADJUSTED GOODNESS OF FIT INDEX IS .849
 ROOT MEAN SQUARE RESIDUAL IS .122

Appendix B.2
Confirmatory First-Order Solution Positioning Correlated Factors
(n=487, y=18)

LAMBDA X Item	LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE
Eros 2	.000	.622	.000	.000	.000	.000
Ludus 8	.769	.600	.000	.000	.000	.000
Storge18	.000	.000	.906	.000	.000	.000
Pragma25	.000	.000	.000	.000	.689	.000
Mania 33	.000	.000	.000	.654	.000	.000
Agape 38	.000	.000	.000	.000	.000	.687
Pragma27	.000	.000	.000	.000	.500	.000
Eros 4	.000	.796	.000	.000	.000	.000
Storge21	.000	.000	.620	.000	.000	.000
Agape 39	.000	.000	.000	.000	.000	.705
Mania 32	.000	.000	.000	.713	.000	.000
Ludus 14	.547	.000	.000	.000	.000	.000
Agape 42	.000	.000	.000	.000	.000	.713
Mania 31	.000	.000	.000	.640	.000	.000
Pragma26	.000	.000	.000	.000	.431	.000
Storge20	.000	.000	.344	.000	.000	.000
Ludus 9	.384	.000	.000	.000	.000	.000
Eros 7	.000	.474	.000	.000	.000	.000

PHI	LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE
LUDUS	1.000					
EROS	-.238	1.000				
STORGE	.077	.067	1.000			
MANIA	.358	.165	.061	1.000		
PRAGMA	.335	.125	.234	.404	1.000	
AGAPE	-.128	.385	.105	.645	.321	1.000

MEASURES OF GOODNESS OF FIT FOR THE WHOLE MODEL:
 CHI-SQUARE WITH 120 DEGREES OF FREEDOM IS 285.92 (PROB.
 LEVEL = .000)
 GOODNESS OF FIT INDEX IS .938
 ADJUSTED GOODNESS OF FIT INDEX IS .912
 ROOT MEAN SQUARE RESIDUAL IS .056

Appendix B.3
Confirmatory First-Order Solution Positing Uncorrelated Factors
(n=260 from Thompson & Borrello, 1987, y=18)

LAMBDA X Item	LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE
Eros 2	.000	.638	.000	.000	.000	.000
Ludus 8	.600	.000	.000	.000	.000	.000
Storge18	.000	.000	.925	.000	.000	.000
Pragma25	.000	.000	.000	.000	.945	.000
Mania 33	.000	.000	.000	.657	.000	.000
Agape 38	.000	.000	.000	.000	.000	.768
Pragma27	.000	.000	.000	.000	.445	.000
Eros 4	.000	.778	.000	.000	.000	.000
Storge21	.000	.000	.587	.000	.000	.000
Agape 39	.000	.000	.000	.000	.000	.686
Mania 32	.000	.000	.000	.649	.000	.000
Ludus 14	.718	.000	.000	.000	.000	.000
Agape 42	.000	.000	.000	.000	.000	.644
Mania 31	.000	.000	.000	.733	.000	.000
Pragma26	.000	.000	.000	.000	.385	.000
Storge20	.000	.000	.411	.000	.000	.000
Ludus 9	.358	.000	.000	.000	.000	.000
Eros 7	.000	.438	.000	.000	.000	.000

MEASURES OF GOODNESS OF FIT FOR THE WHOLE MODEL:
 CHI-SQUARE WITH 135 DEGREES OF FREEDOM IS 446.60 (PROB.
 LEVEL = .000)
 GOODNESS OF FIT INDEX IS .837
 ADJUSTED GOODNESS OF FIT INDEX IS .793

Appendix B.4
Confirmatory First-Order Solution Positing Correlated Factors
(n=260 from Thompson & Borrello, 1987, y=18)

LAMBDA X							
Item		LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE
Eros 2		.000	.647	.000	.000	.000	.000
Ludus 8		.734	.000	.000	.000	.000	.000
Storge18		.000	.000	.903	.000	.000	.000
Pragma25		.000	.000	.000	.000	.801	.000
Mania 33		.000	.000	.000	.643	.000	.000
Agape 38		.000	.000	.000	.000	.000	.720
Pragma27		.000	.000	.000	.000	.500	.000
Eros 4		.000	.765	.000	.000	.000	.000
Storge21		.000	.000	.600	.000	.000	.000
Agape 39		.000	.000	.000	.000	.000	.681
Mania 32		.000	.000	.000	.690	.000	.000
Ludus 14		.590	.000	.000	.000	.000	.000
Agape 42		.000	.000	.000	.000	.000	.697
Mania 31		.000	.000	.000	.705	.000	.000
Pragma26		.000	.000	.000	.000	.462	.000
Storge20		.000	.000	.420	.000	.000	.000
Ludus 9		.332	.000	.000	.000	.000	.000
Eros 7		.000	.443	.000	.000	.000	.000

PHI							
		LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE
LUDUS		1.000					
EROS		-.210	1.000				
STORGE		.121	.013	1.000			
MANIA		.379	.270	.080	1.000		
PRAGMA		.278	.142	.267	.381	1.000	
AGAPE		-.089	.460	.179	.718	.408	1.000

MEASURES OF GOODNESS OF FIT FOR THE WHOLE MODEL:
CHI-SQUARE WITH 120 DEGREES OF FREEDOM IS 246.79 (PROB.
LEVEL = .000)
GOODNESS OF FIT INDEX IS .905
ADJUSTED GOODNESS OF FIT INDEX IS .864
ROOT MEAN SQUARE RESIDUAL IS .068

Appendix B.5
Confirmatory Second-Order Solution
(n=260 from Thompson & Borrello, 1987, Y=18)

LAMBDA Y Item	LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE	LOVE G
Eros 2	.000	.850	.000	.000	.000	.000	.000
Ludus 8	.800	.000	.000	.000	.000	.000	.000
Storge18	.000	.000	1.000	.000	.000	.000	.000
Pragma25	.000	.000	.000	.000	1.000	.000	.000
Mania 33	.000	.000	.000	.902	.000	.000	.000
Agape 38	.000	.000	.000	.000	.000	1.000	.000
Pragma27	.000	.000	.000	.000	.568	.000	.000
Eros 4	.000	1.000	.000	.000	.000	.000	.000
Storge21	.000	.000	.727	.000	.000	.000	.000
Agape 39	.000	.000	.000	.000	.000	.940	.000
Mania 32	.000	.000	.000	.988	.000	.000	.000
Ludus 14	1.000	.000	.000	.000	.000	.000	.000
Agape 42	.000	.000	.000	.000	.000	.935	.000
Mania 31	.000	.000	.000	1.000	.000	.000	.000
Pragma26	.000	.000	.000	.000	.528	.000	.000
Storge20	.000	.000	.492	.000	.000	.000	.000
Ludus 9	.477	.000	.000	.000	.000	.000	.000
Eros 7	.000	.616	.000	.000	.000	.000	.000

BETA

	LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE	LOVE G
LUDUS	.000	.000	.000	.000	.000	.000	.087
EROS	.000	.000	.000	.000	.000	.000	.474
STORGE	.000	.000	.000	.000	.000	.000	.250
MANIA	.000	.000	.000	.000	.000	.000	.762
PRAGMA	.000	.000	.000	.000	.000	.000	.530
AGAPE	.000	.000	.000	.000	.000	.000	1.000
LOVE G	.000	.000	.000	.000	.000	.000	.000

PSI

	LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE	LOVE G
LUDUS	.537						
EROS	.000	.461					
STORGE	.000	.000	.719				
MANIA	.000	.000	.000	.215			
PRAGMA	.000	.000	.000	.000	.574		
AGAPE	.000	.000	.000	.000	.000	.049	
LOVE G	.000	.000	.000	.000	.000	.000	.484

MEASURES OF GOODNESS OF FIT FOR THE WHOLE MODEL:
CHI-SQUARE WITH 129 DEGREES OF FREEDOM IS 303.03 (PROB.
LEVEL = .000)
GOODNESS OF FIT INDEX IS .880
ADJUSTED GOODNESS OF FIT INDEX IS .841
ROOT MEAN SQUARE RESIDUAL IS .083

Appendix B.6
Confirmatory First-Order Solution Positing Correlated Factors
($n=227$ from Borrello & Thompson, 1987, [$n=176$]
and Borrello & Thompson, 1989a, [$n=51$] $y=20$)

LAMBDA X Item	LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE
Eros 2	.000	.607	.000	.000	.000	.000
Ludus 8	.793	.000	.000	.000	.000	.000
Storge18	.000	.000	.965	.000	.000	.000
Pragma25	.000	.000	.000	.000	.546	.000
Mania 33	.000	.000	.000	.674	.000	.000
Agape 38	.000	.000	.000	.000	.000	.636
Pragma27	.000	.000	.000	.000	.511	.000
Eros 4	.000	.813	.000	.000	.000	.000
Storge21	.000	.000	.605	.000	.000	.000
Agape 39	.000	.000	.000	.000	.000	.702
Mania 32	.000	.000	.000	.742	.000	.000
Ludus 14	.518	.000	.000	.000	.000	.000
Agape 42	.000	.000	.000	.000	.000	.775
Mania 31	.000	.000	.000	.575	.000	.000
Pragma26	.000	.000	.000	.000	.378	.000
Storge20	.000	.000	.257	.000	.000	.000
Ludus 9	.445	.000	.000	.000	.000	.000
Eros 7	.000	.522	.000	.000	.000	.000
Agape 37	.000	.000	.000	.000	.000	.684
Mania 34	.000	.000	.000	.192	.000	.000

PHI	LUDUS	EROS	STORGE	MANIA	PRAGMA	AGAPE
LUDUS	1.000					
EROS	-.263	1.000				
STORGE	.038	.104	1.000			
MANIA	.342	.066	.036	1.000		
PRAGMA	.394	.105	.215	.425	1.000	
AGAPE	-.188	.328	.018	.534	.148	1.000

MEASURES OF GOODNESS OF FIT FOR THE WHOLE MODEL:
CHI-SQUARE WITH 155 DEGREES OF FREEDOM IS 217.92 (PROB.
LEVEL = .001)
GOODNESS OF FIT INDEX IS .913
ADJUSTED GOODNESS OF FIT INDEX IS .882
ROOT MEAN SQUARE RESIDUAL IS .063